

- (1) Two spring strips with different thermal expansion coefficients  $\alpha_1$  and  $\alpha_2$  are firmly welded together as a welded bimetallic strip, as shown in Fig.1. The thermal expansion coefficient  $\alpha_1$  is  $1.2 \times \alpha_2$ . The both spring strips have the same length  $L$ , thickness  $H$ , and width  $W$ , and they have also the same Young's Modulus  $E$ .  
 (Hint:  $H$  and  $W$  are significantly smaller than  $L$ ; therefore it is assumed that the thermal expansion affects only the length  $L$ )
- (a) Determine the longitudinal stiffness of each "unwelded" spring strip,  $k_1$  and  $k_2$ . (4%)
- (b) When the temperature increase  $\Delta T$ ,
- (b-1) determine the thermal induced longitudinal expansion of each "unwelded" spring strip,  $\Delta l_1$  and  $\Delta l_2$ . (4%)
- (b-2) determine the moment distribution  $M$  along the whole length  $x$  of the welded bimetallic strip. (8%)

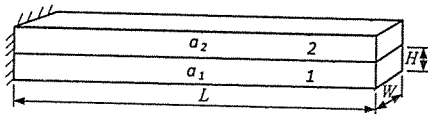


Fig. 1 Welded bimetallic strip

- (2) A block brake with the hinge location C is shown in Fig.2. A pneumatic actuator with the piston diameter  $D$  and rod diameter  $d$  is driven by air pressures of  $P_1$  and  $P_2$  to generate the actuating force  $F_a$  at the end of the actuating lever. However there is also a friction force  $F_f$  between the piston and the cylinder tube against their relative motion. The friction coefficient between the brake lining and the drum is  $\mu$ .

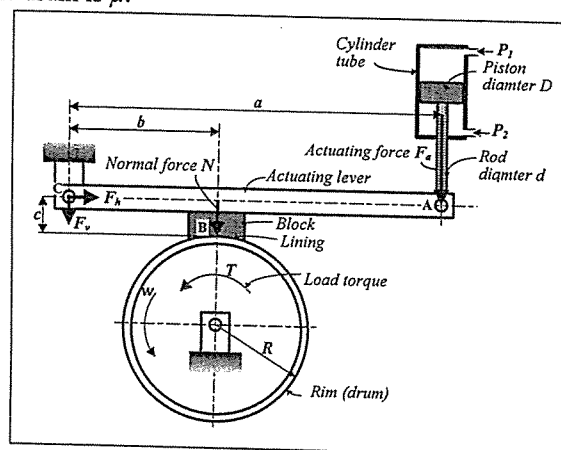
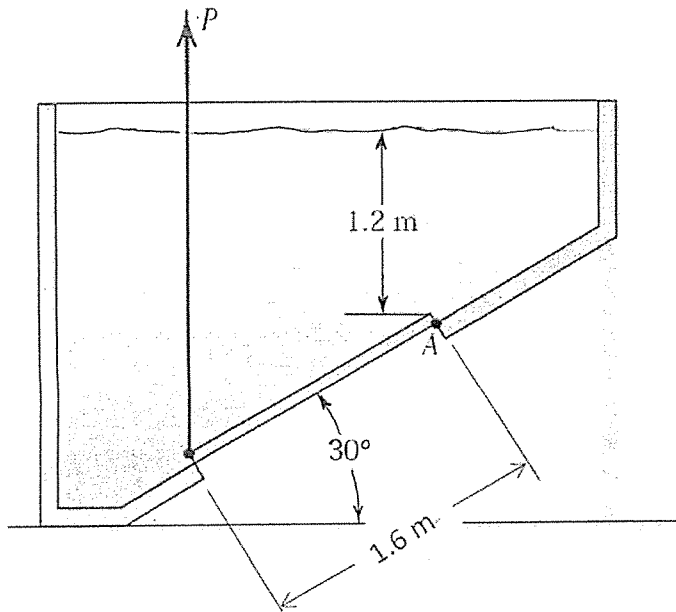


Fig.2 Block brake

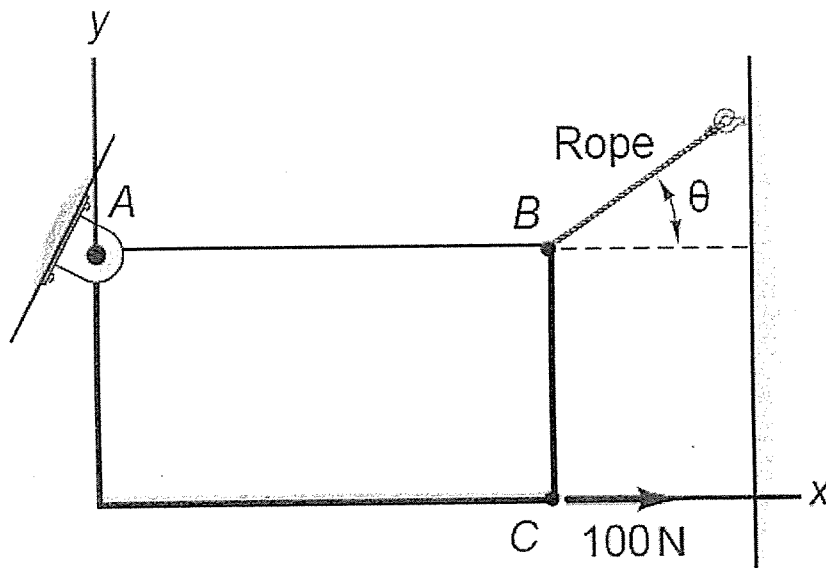
- Please derive the following parameters with the above-mentioned dimensional parameters.
- (a) The actuating force  $F_a$  of the pneumatic actuator, (4%)
- (b) The normal force  $N$  between the lining and the drum, (4%)
- (c) The horizontal and vertical reaction forces,  $F_h$  and  $F_v$ , on the pin location C, (4%)
- (d) The braking torque  $T_b$  on the drum, (4%)

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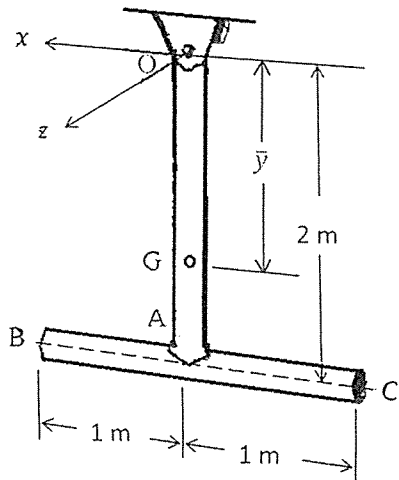
- (3). The cross section of a fresh water tank with a slanted bottom is shown. A rectangular door 1.6 x 0.8 m in the bottom of the tank is hinged at A and is opened against the pressure of the water by the cable under a tension P as shown. The specific weight of fresh water is  $1000 \text{ kg/m}^3$ . Calculate P. (10%)



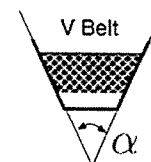
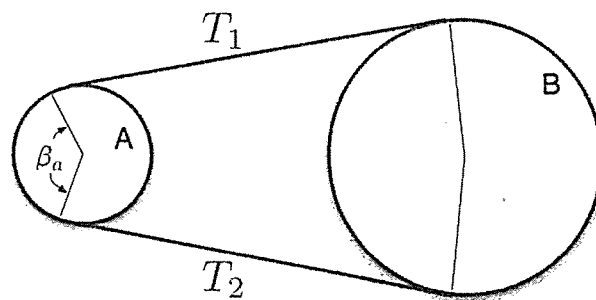
- (4). A 300-N weight of block is held in place by a pin at A and a rope at B. The block is 2 m by 1 m and its center of gravity is located at its geometric center. A 100-N horizontal force is applied at point C. Discuss the solution for the cases: (a)  $\theta$  is not specified, (b)  $\theta = 0^\circ$ , and (c)  $\theta = 30^\circ$ . (10%)



- (5). A pendulum consists of two thin rods each having a weight of 10 N. Determine the pendulum's mass moment of inertia about an axis parallel to z-axis and passing through (a) the pin at O, and (b) the mass center G of the pendulum. (10%)



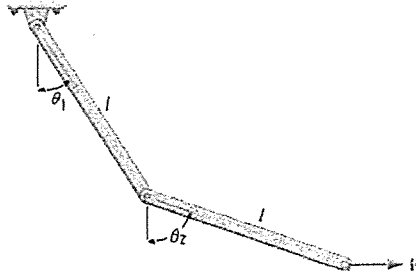
- (6) Consider the belt drive as shown in figure. Pulley B drives pulley A clockwise. The radius for pulleys A and B are  $R_A$  and  $R_B$ , respectively. The coefficient of friction between the belt and the pulley is  $\mu$ .



- (a) Please derive the relationships between  $T_1$  and  $T_2$  for flat belt. (8%)  
 (b) Please derive the relationships between  $T_1$  and  $T_2$  for v-belt. (10%)

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- (7) Figure shows a simplified diagram of a robot arm in vehicle assembly plants. Consider a manufacturing task which results in a horizontal force  $P$  as shown. Please determine the angles  $\theta_1$  and  $\theta_2$  for equilibrium of the two links. Assume each link is uniform with a mass  $m$ . (20%)



試題隨卷繳回